

## Physics of Roller Coasters

### Lesson Notes

#### Learning Outcomes

- How does Physics explain the thrills of a roller coaster ride?
- How can Newton's Laws be used to analyze the roller coaster experience?

#### The Physics Behind the Phun

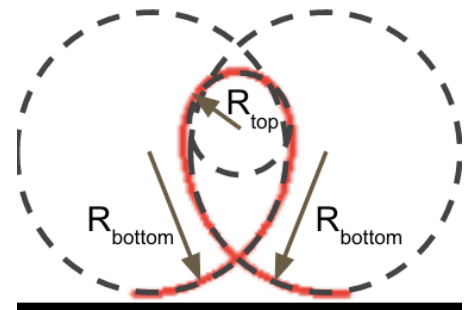
- It's not about the speed!
- It's about the acceleration and the sensations of weightlessness and weightiness associated with the accelerations.

#### Clothoid Loops

There are two safety issues with looping coasters:

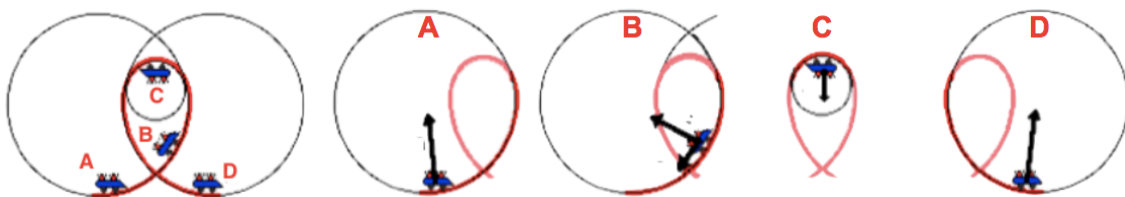
- At loop bottom:  $a$  cannot be too large or riders will black out.
- At the loop top:  $a \geq 9.8 \text{ m/s}^2$ .

The tear-dropped shape loops are known as **clothoid loops**. They have a continuously changing radius. The radius at the bottom is significantly larger than that at the top. Accelerations decrease when the turning radius is larger. ( $a = v^2/R$ )



#### Accelerations in the Loops

The magnitude and direction of a rider's velocity (in blue) is constantly changing. This is the cause of acceleration. The accelerations in the loop have a centripetal (inward) component due to the direction change and a tangential component due to the speed change.



#### Normal Force

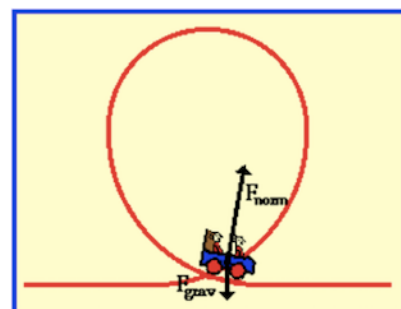
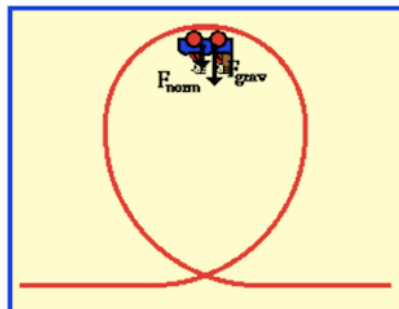
The normal force varies in size and direction.

##### Loop Top:

$F_{\text{grav}}$  and  $F_{\text{norm}}$  are both inward.

##### Loop Bottom:

$F_{\text{grav}}$  is outward and  $F_{\text{norm}}$  is inward.



Show your solutions to Example Problems 1, 2, and 3. (Example 3 is on Slide 11.)

**Example 1 - Analysis of a Loop Top**

Anna Litical experiences a downward acceleration of  $15.6 \text{ m/s}^2$  at the top of a loop. Determine the normal force acting upon Anna's 48.5-kg body.

**Example 2 - Analysis of a Loop Bottom**

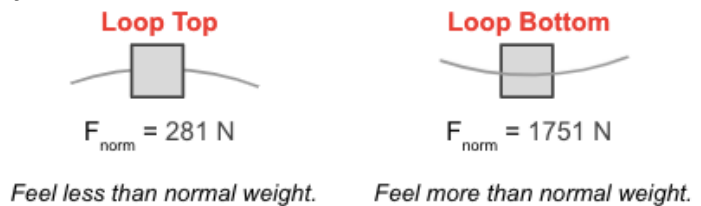
Anna Litical experiences a downward acceleration of  $15.6 \text{ m/s}^2$  at the top of a loop. Determine the normal force acting upon Anna's 48.5-kg body.

**Example 3 - Analysis of a Hill Top**

Anna Litical is moving at  $18.9 \text{ m/s}$  over the crest of a hill that has a radius of curvature of  $24.8 \text{ m}$ . The safety bar applies a downward force on her body. Determine this applied force that acts on Anna's 48.5-kg body.

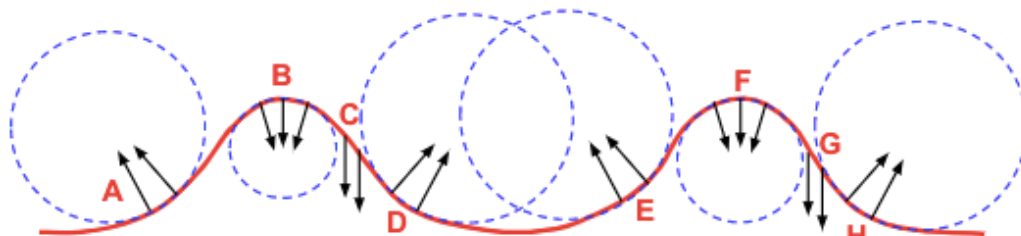
**The Normal Force as a Thrill Factor**

- The force of gravity on our bodies - our *weight* - cannot be felt. We only feel the contact forces that counteract the force of gravity.
- Our sense of how much we weigh is based on our feel for these contact forces - usually  $F_{\text{norm}}$ .
- Usually 48.5 kg Anna feels 475 N of normal force.



**Hills and Dips**

The dips and hills of a coaster ride blend circular motion and free fall experiences. The thrill results from the accelerations and the sensations of weightlessness and weightiness.



Locations **B** and **F**: Partial weightlessness or negative Gs.

Locations **C** and **G**: Weightlessness; free fall.

Locations **D** and **H** (also **A** and **E**): feelings of weightiness; large # of Gs.