

## DeciBels and Intensity Calculations

### Lesson Notes

#### Learning Outcomes

- How do you calculate the deciBel rating from the intensity value and vice versa?
- How do changes in the distance from the source factor into these calculations?

#### The Equations

The deciBel scale is a logarithmic scale that compares the intensity of a sound to the intensity of the **threshold of hearing** ( $1.0 \times 10^{-12} \text{ W/m}^2$ ).

$$\text{dB} = 10 \cdot \log (I / I_0) \quad \text{where } I = \text{intensity of sound}$$

$$I_0 = 1.0 \times 10^{-12} \text{ W/m}^2$$

The intensity of a sound ( $I$ ) can be calculated from its deciBel rating ( $\text{dB}$ ) using the equation ...

$$I = I_0 \cdot 10^x \quad \text{where } I_0 = 1.0 \times 10^{-12} \text{ W/m}^2$$

$$x = \text{dB}/10$$

Watch the video and show your organized solutions to the following example problems:

#### Example 1

Determine the deciBel rating of a sound that has an intensity level of  $2.85 \times 10^{-5} \text{ W/m}^2$ .

$$\text{dB} = 10 \cdot \log (I / I_0)$$

dB = deciBel rating  
 $I$  = intensity ( $\text{W/m}^2$ )  
 $I_0 = 1.0 \times 10^{-12} \text{ W/m}^2$   
 Log: a button on your calculator

#### Example 2

Determine the intensity of a sound that has an deciBel rating of 97.2 dB.

$$I = I_0 \cdot 10^x$$

$I$  = intensity ( $\text{W/m}^2$ )  
 $I_0 = 1.0 \times 10^{-12} \text{ W/m}^2$   
 $x = \text{dB}/10$   
 dB = deciBel rating

#### Intensity, Distance, and Power

The intensity ( $I$ ) of a sound at any distance ( $R$ ) from the sound source with power ( $P$ ) is given by the equation ...

$$I = \frac{P}{4 \cdot \pi \cdot R^2}$$

$P$  is a property of the sound source (Watts).  $R$  is the distance from the source (in meters).  $I$  is the intensity in  $\text{W/m}^2$ .

The intensity-distance relationship is often written as a proportionality statement:

$$I \propto \frac{1}{R^2}$$

- Doubling  $R \Rightarrow I$  becomes 1/4-th the original value
- Tripling  $R \Rightarrow I$  becomes 1/9-th the original value
- Halving  $R \Rightarrow I$  becomes 4 times the original value

**Example 3**

Determine the intensity a distance of 2.8 m from the 450-Watt speakers in your room.

**Example 4**

The intensity a distance of 1.6 m from a source is  $7.2 \times 10^{-4} \text{ W/m}^2$ . Determine the intensity a distance of ...

a. 3.2 m from the source:

4.8 m from the source:

6.4 m from the source:

**Example 5**

The deciBel rating a distance of 1.6 m from a source is 54.2 dB. Determine the deciBel rating a distance of ...

a. 3.2 m from the source:

b. 4.8 m from the source:

c. 6.4 m from the source: